

Name:..... Section: ID Number:.....

Q1: Evaluate the indicated limit, or show that it does not exist. *(2 points each)*

$$(i) \lim_{(x,y) \rightarrow (2,1)} \frac{x^2 - 4y^2}{2y - x} \qquad (ii) \lim_{(x,y) \rightarrow (0,0)} \frac{3y^2}{x^2 + y^2}.$$

Q2: Find the domain of the function *(3 points)*

$$f(x, y, z) = \frac{x^2 + 2xy - z}{x + y - z}.$$

\Rightarrow Please Continue

Q3: Use linear approximation to approximate the function

(3 points each)

$$f(x, y) = \sin(x + y) \quad \text{at the point} \quad \left(\frac{\pi}{6}, \frac{\pi}{12}\right).$$

Q4: Show that if $f(x, y) = \sin(3\pi x) \cos(6\pi y)$, then

(5 points)

$$4 \frac{\partial^2 f}{\partial x^2} - \frac{\partial^2 f}{\partial y^2} = 0.$$